

Equations

$$\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial y^2} - \Gamma \frac{\partial^3 u}{\partial y^2 \partial t} + Gr\theta,$$

$$\text{Pr} \frac{\partial \theta}{\partial t} = \frac{\partial^2 \theta}{\partial y^2},$$

$$u(y, 0) = 0, \quad \theta(y, 0) = 0; \quad y > 0,$$

$$u(0, t) = 0, \quad u(\infty, t) = 0, \quad \theta(0, t) = 1, \quad \theta(\infty, t) = 0,$$

> restart :

> with(plots) :

$$\begin{aligned} > PDE := \left\{ \frac{\partial}{\partial t} u(y, t) = \frac{\partial^2}{\partial y^2} u(y, t) + R \left(\frac{\partial^3}{\partial t \partial y^2} u(y, t) \right) + Gr \cdot z(y, t), \right. \\ & \left. Pr \left(\frac{\partial}{\partial t} z(y, t) \right) = \frac{\partial^2}{\partial y^2} z(y, t) \right\}; \end{aligned}$$

$$\begin{aligned} & PDE := \left\{ Pr \left(\frac{\partial}{\partial t} z(y, t) \right) = \frac{\partial^2}{\partial y^2} z(y, t), \frac{\partial}{\partial t} u(y, t) = \frac{\partial^2}{\partial y^2} u(y, t) \right. \\ & \left. + R \left(\frac{\partial^3}{\partial y^2 \partial t} u(y, t) \right) + Gr z(y, t) \right\} \end{aligned}$$

$$\begin{aligned} > IBC := \{u(y, 0) = 0, u(0, t) = 0, u(10, t) = 0, z(y, 0) = 0, z(0, t) = 1, \\ & z(10, t) = 0\}; \end{aligned}$$

$$\begin{aligned} & IBC := \{u(0, t) = 0, u(10, t) = 0, u(y, 0) = 0, z(0, t) = 1, z(10, t) = 0, \\ & z(y, 0) = 0\} \end{aligned}$$

> Pr := 0.71; R := 0.2;

$$Pr := 0.71$$

$$R := 0.2$$

> for i from 1 by 1 to 4 do
 $Gr := L[i]: pds := \text{pdsolve}\left(PDE, IBC,$
 $\text{numeric, spacestep} = \frac{1}{100}\right)$:
 $p[i] := \text{plots}[display]\left(\left[\text{seq}\left(pds:-\right.$
 $\text{plot}\left(u, t = \frac{j}{10}, y = 0..6, \text{legend} = [i]\right), j = 4\right]\right)$:
end do

> $\text{display}(\{p[1], p[2], p[3], p[4]\});$

