

> restart # solve with variable epsilon

$$\begin{aligned} > \text{eq3} := 2 \cdot d_2 + \frac{6 \cdot d_3 \cdot 11}{3} = & \frac{\left(d_1 + \frac{2 \cdot d_2 \cdot 11}{3} + 3 \cdot d_3 \cdot \left(\frac{11}{3}\right)^2\right)^2}{d_0 + \frac{d_1 \cdot 11}{3} + d_2 \cdot \left(\frac{11}{3}\right)^2 + d_3 \cdot \left(\frac{11}{3}\right)^3} \\ & - \frac{\epsilon \cdot \left(d_0 + \frac{d_1 \cdot 11}{3} + d_2 \cdot \left(\frac{11}{3}\right)^2 + d_3 \cdot \left(\frac{11}{3}\right)^3\right)}{\left(\frac{11}{3}\right)^2} : \end{aligned}$$

$$\begin{aligned} > \text{eq4} := 2 \cdot d_2 + \frac{6 \cdot d_3 \cdot 19}{3} = & \frac{\left(d_1 + \frac{2 \cdot d_2 \cdot 19}{3} + 3 \cdot d_3 \cdot \left(\frac{19}{3}\right)^2\right)^2}{d_0 + \frac{d_1 \cdot 19}{3} + d_2 \cdot \left(\frac{19}{3}\right)^2 + d_3 \cdot \left(\frac{19}{3}\right)^3} \\ & - \frac{\epsilon \cdot \left(d_0 + \frac{d_1 \cdot 19}{3} + d_2 \cdot \left(\frac{19}{3}\right)^2 + d_3 \cdot \left(\frac{19}{3}\right)^3\right)}{\left(\frac{19}{3}\right)^2} : \end{aligned}$$

$$> \text{eq5} := d_0 + d_1 + d_2 + d_3 = 8 :$$

$$> \text{eq6} := d_0 + d_1 \cdot 9 + d_2 \cdot 9^2 + d_3 \cdot 9^3 = 2 :$$

> solve({eq3, eq4, eq5, eq6}, {d₀, d₁, d₂, d₃}) assuming ε :: real :

> assign(%)

> ε := -0.1

$$\epsilon := -0.1 \tag{1}$$

> simplify(d₀)

$$12.4284775514022 - 4.45119223219462 \text{ I} \tag{2}$$

> restart # fsolve without variable epsilon

$$\begin{aligned} > \text{eq3} := 2 \cdot d_2 + \frac{6 \cdot d_3 \cdot 11}{3} = & \frac{\left(d_1 + \frac{2 \cdot d_2 \cdot 11}{3} + 3 \cdot d_3 \cdot \left(\frac{11}{3}\right)^2\right)^2}{d_0 + \frac{d_1 \cdot 11}{3} + d_2 \cdot \left(\frac{11}{3}\right)^2 + d_3 \cdot \left(\frac{11}{3}\right)^3} \\ & - \frac{\epsilon \cdot \left(d_0 + \frac{d_1 \cdot 11}{3} + d_2 \cdot \left(\frac{11}{3}\right)^2 + d_3 \cdot \left(\frac{11}{3}\right)^3\right)}{\left(\frac{11}{3}\right)^2} : \end{aligned}$$

$$\begin{aligned} > \text{eq4} := 2 \cdot d_2 + \frac{6 \cdot d_3 \cdot 19}{3} = & \frac{\left(d_1 + \frac{2 \cdot d_2 \cdot 19}{3} + 3 \cdot d_3 \cdot \left(\frac{19}{3}\right)^2\right)^2}{d_0 + \frac{d_1 \cdot 19}{3} + d_2 \cdot \left(\frac{19}{3}\right)^2 + d_3 \cdot \left(\frac{19}{3}\right)^3} \end{aligned}$$

$$-\frac{\epsilon \cdot \left(d_0 + \frac{d_1 \cdot 19}{3} + d_2 \cdot \left(\frac{19}{3}\right)^2 + d_3 \cdot \left(\frac{19}{3}\right)^3\right)}{\left(\frac{19}{3}\right)^2} :$$

(3)

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> eq5 := d0 + d1 + d2 + d3 = 8 :
> eq6 := d0 + d1 · 9 + d2 · 92 + d3 · 93 = 2 :
> ε := -0.1
      ε := -0.1

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(3)

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> fsolve( {eq3, eq4, eq5, eq6}, {d0, d1, d2, d3} ) assuming ε :: real :
> assign(%)
> simplify( d0)

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(4)

9.660121266