

Steps output from Integration,  
Contradictory expressions in red text.

$$\begin{aligned}
 & \int 2\sqrt{x} \sqrt{1 + \frac{1}{x}} \, dx \\
 &= \int 2\sqrt{x+1} \, dx \quad \left[ \text{rewrite, } 2\sqrt{x} \sqrt{1 + \frac{1}{x}} = 2\sqrt{x+1} \right] \\
 &= 2 \left( \int \sqrt{x+1} \, dx \right) \quad [\text{constant multiple}]
 \end{aligned} \tag{1}$$

$$\int 2\sqrt{x} \sqrt{1 + \frac{1}{x}} \, dx = 2 \left( \int \sqrt{x+1} \, dx \right) \tag{1}$$

$$\xrightarrow{\text{test relation}} \quad \text{false} \tag{2}$$

$$2\sqrt{x} \sqrt{1 + \frac{1}{x}} = 2\sqrt{x+1} \xrightarrow{\text{test relation}} \text{false}$$