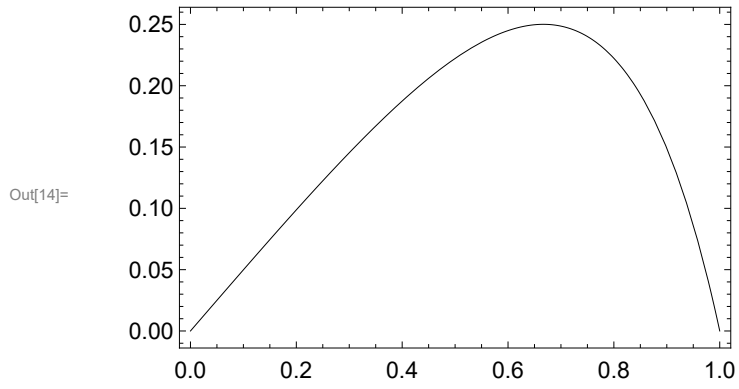


```

In[1]:= k = 2;
a = 0.5;
a1 =  $\frac{(a^2 - 1)}{2}$ ; (*0.1,0.5,1,3*)
a2 = (a^2 - 1) a1;
We = 0;
x[1] = 0;
H = .666667;
For[ii = 1, ii ≤ 11, ii++,
  h = k - (k - 1) * x[ii];
  sol = NDSolve[{D[(u''[y] + We^2 a1 (u''[y])^3 + We^4 a2 (u''[y])^5), y, y] == 0, u[0] == 0,
    u'[0] == 1, u[h] == H, u'[h] == 0}, {u[y], u'[y], u''[y], u'''[y]}, {y, 0, h}];
  ppx = Table[(u^(3)[y] + 3 a1 We^2 u''[y]^2 u^(3)[y] + 5 a2 We^4 u''[y]^4 u^(3)[y]) /. sol,
    {y, 0, h, 0.1}];
  px[ii] = (u^(3)[y] + 3 a1 We^2 u''[y]^2 u^(3)[y] + 5 a2 We^4 u''[y]^4 u^(3)[y]) /. sol /. y → 0;
  x[ii + 1] = x[ii] + 0.1;
];
tt = Table[{x[ii], px[ii][[1]]}, {ii, 1, 11}];
fff = Interpolation[tt];
ggg = Integrate[Interpolation[tt][x], x];
hhh = Integrate[ggg, {x, 0, 1}];
Table[ggg, {x, 1, 1}]
(*pressure*)
Plot[ggg, {x, 0, 1}, Frame → True,
  PlotStyle → {{Thin, Black}}, LabelStyle → Directive[Black, 12],
  FrameLabel → {"", "", " ", ""}, FrameStyle → Directive[Thin],
  LabelStyle → Directive[18], Epilog → {Arrow[{{}}, {}], Text[""]}];
(*pressure gradient*)
Plot[fff[x], {x, 0, 1}, Frame → True, PlotRange → All,
  PlotStyle → {{Thick, Black}}, LabelStyle → Directive[Black, 12],
  FrameLabel → {"", "", " dp/px ", ""}, FrameStyle → Directive[Thin],
  LabelStyle → Directive[18], Epilog → {Arrow[{{}}, {}], Text[""]}];
(*velocity*)
Plot[u'[y] /. sol, {y, 0, h}, Frame → True,
  PlotStyle → {{Thick, Black}}, LabelStyle → Directive[Black, 12],
  FrameLabel → {"", "", " v ", ""}, FrameStyle → Directive[Thin],
  LabelStyle → Directive[18], Epilog → {Arrow[{{}}, {}], Text[""]}];

```

Out[13]= {0.0000240368}



```
In[17]:= p111 =  $\frac{\text{cer2}[0., 0.]}{0.06 \cdot \text{Spacer2}[0]}$ ;
```

In[18]:= a = 0.5;

η = 1;

μ = 1;

k = 2; (\*0,0.2,0.3\*)

b = 0;

$$\alpha_1 = \frac{(a^2 - 1) \eta}{(\eta + \mu)}; (*0.1,0.5,1,3*)$$

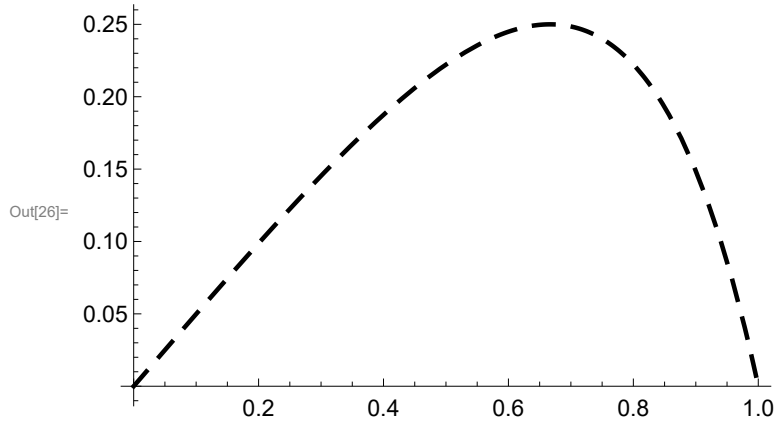
$$\alpha_2 = (a^2 - 1) \alpha_1;$$

$$pp = -\frac{6(-1+k)(-1+x)x}{(1+k)(k+x-kx)^2} -$$

$$\frac{1}{25k(1+k)^3(k+x-kx)^6} 12b^2(-1+k)(-1+x)x(k^3(79+k(-32+k(77+26k))) - (-1+k)k^2(63+k(55+k(191+91k)))x + 3(-1+k)^2k(29+k(49+k(53+39k))))x^2 - (-1+k)^3(1+5k)(13+k(8+13k))x^3 + (-1+k)^4(13+k(8+13k))x^4) \alpha_1 +$$

$$\frac{1}{30625k^3(1+k)^5(k+x-kx)^{10}} 8b^4(-1+k)(-1+x)x(9(-1+k)^2(26164k^{12}(-2+x)(-1+x)^7 + 26164x^7(1+x) + kx^6(209312 + (26439 - 235201x)x) - k^{11}(-1+x)^6(-550 + x(-443963 + 235201x))) + 2k^{10}(-1+x)^5(-10945 + x(75985 + x(-906523 + 487927x))) + 2k^2x^5(353556 + x(-273280 + x(-557258 + 487927x))) + 4k^6(-1+x)x(-168418 + (-1+x)x(-476296 + (-1+x)x(346861 + 1655413(-1+x)x))) - 5k^3x^4(-282331 + x(438137 + x(341729 + x(-1035337 + 498297x)))) - 5k^9(-1+x)^4(-39505 + x(-8772 + x(225500 + x(-957851 + 498297x)))) + 20k^4x^3(85379 + x(-199689 + x(-23569 + x(560189 + 11x(-58191 + 20203x)))))) + 20k^8(-1+x)^3(-4442 + x(-15499 + x(-38722 + x(222115 + 11x(-42824 + 20203x)))))) + k^5x^2(1427274 + x(-4230511 + 2x(872810 + x(6586595 + x(-13525745 + (10584551 - 3015409x)x)))))) - k^7(-1+x)^2(-202367 + x(234941 + 2x(-92500 + x(-1979055 + x(5834125 + x(-7507903 + 3015409x))))))))) \alpha_1^2 - 250(2k^7(3616 + k(-4429 + k(4302 + k(-3193 + k(2038 + k(1683 + k(-1031 + 689k))))))) - (-1+k)k^6(17267 + k(-21021 + k(15543 + k(-6983 + k(14973 + k(25929 + k(-16843 + 10335k)))))))x + (-1+k)^2k^5(40814 + k(-38829 + k(11524 + k(44317 + k(9938 + k(88291 + k(-59476 + 33761k)))))))x^2 - (-1+k)^3k^4(46410 + k(-31846 + k(-1865 + k(138739 + k(-36884 + k(173044 + 13k(-9125 + 4823k)))))))x^3 + (-1+k)^4k^3(40306 + k(-994 + k(-37264 + k(190331 + k(-92344 + 5k(42550 + k(-29230 + 14469k)))))))x^4 - (-1+k)^5k^2(19292 + k(11438 + k(-58254 + k(155082 + k(-97575 + k(167361 + k(-113837 + 53053k)))))))x^5 + (-1+k)^6k(5512 + k(11044 + k(-38486 + k(78060 + k(-56266 + k(81919 + k(-54688 + 24115k)))))))x^6 - (-1+k)^7(1+9k)(689 + k(-1720 + k(2714 + k(-2228 + k(2714 + k(-1720 + 689k))))))x^7 + (-1+k)^8(689 + k(-1720 + k(2714 + k(-2228 + k(2714 + k(-1720 + 689k))))))x^8) \alpha_2);$$

Plot[pp, {x, 0, 1}, PlotStyle -> {Thickness[0.007], Dashing[.030], Black}, LabelStyle -> Directive[Black, 12]]



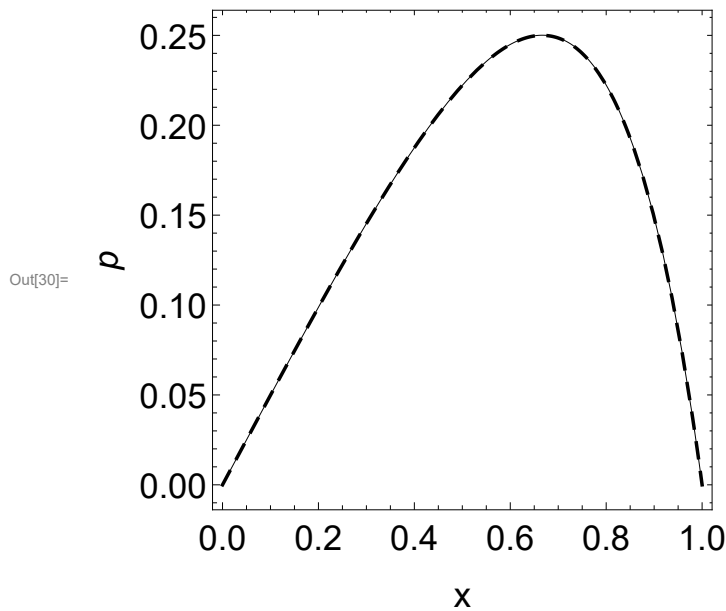
```
In[27]:= p1111 = Plot[0.25 - 0.4 x^2, {x, 0, 1}];
```

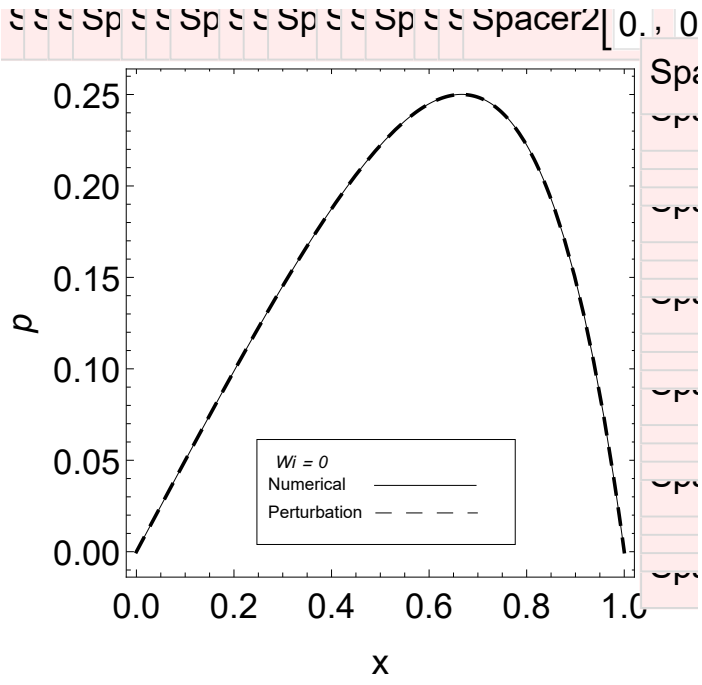
```
In[28]:= p = Plot[0.25 - 0.4 x^2, {x, 0, 1}];
```

```
In[29]:= p22 = Plot[0.25 - 0.4 x^2, {x, 0, 1}];
```

```
In[30]:= Show[{p1111, p1111}, Frame -> True, PlotRange -> All, LabelStyle -> Directive[Black, 18],
  AspectRatio -> 1, FrameLabel -> {"x", "p", " a = 0.5, k = 2", ""},
  FrameStyle -> Directive[Thin], LabelStyle -> Directive[Black, 18], Axes -> False]
```

$a = 0.5, k = 2$





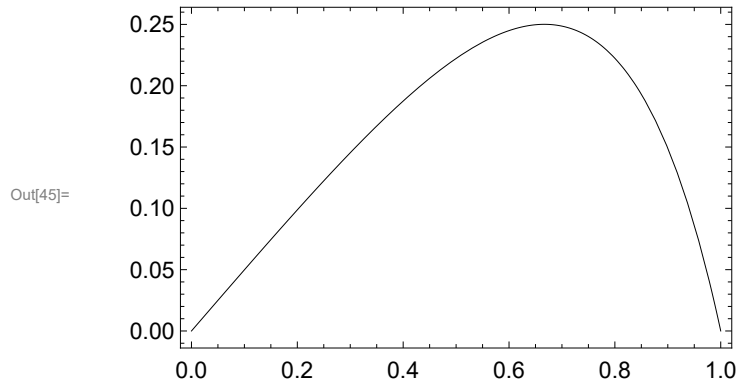
```

In[31]:= k = 2;
a = 0.5;
a1 =  $\frac{(a^2 - 1)}{2}$ ; (*0.1,0.5,1,3*)
a2 = (a^2 - 1) a1;
We = 0;
x[1] = 0;
H = .66667;
For[ii = 1, ii ≤ 11, ii++,
  h = k - (k - 1) * x[ii];
  sol = NDSolve[{D[(u''[y] + We^2 a1 (u''[y])^3 + We^4 a2 (u''[y])^5), y, y] == 0, u[0] == 0,
    u'[0] == 1, u[h] == H, u'[h] == 0}, {u[y], u'[y], u''[y], u'''[y]}, {y, 0, h}];
  ppx = Table[(u^(3)[y] + 3 a1 We^2 u''[y]^2 u^(3)[y] + 5 a2 We^4 u''[y]^4 u^(3)[y]) /. sol,
    {y, 0, h, 0.1}];
  px[ii] = (u^(3)[y] + 3 a1 We^2 u''[y]^2 u^(3)[y] + 5 a2 We^4 u''[y]^4 u^(3)[y]) /. sol /. y → 0;
  x[ii + 1] = x[ii] + 0.1;
];
tt = Table[{x[ii], ppx[ii][[1]]}, {ii, 1, 11}];
fff = Interpolation[tt];
ggg = Integrate[Interpolation[tt][x], x];
hhh = Integrate[ggg, {x, 0, 1}];
Integrate[ggg, {x, 0, 1}]
Table[ggg, {x, 1, 1}]
(*pressure*)
Plot[ggg, {x, 0, 1}, Frame → True,
  PlotStyle → {{Thin, Black}}, LabelStyle → Directive[Black, 12],
  FrameLabel → {"", "", " ", ""}, FrameStyle → Directive[Thin],
  LabelStyle → Directive[18], Epilog → {Arrow[{{}}, {}], Text[""]}];
(*pressure gradient*)
Plot[fff[x], {x, 0, 1}, Frame → True, PlotRange → All,
  PlotStyle → {{Thick, Black}}, LabelStyle → Directive[Black, 12],
  FrameLabel → {"", "", " dp/pX ", ""}, FrameStyle → Directive[Thin],
  LabelStyle → Directive[18], Epilog → {Arrow[{{}}, {}], Text[""]}];
(*velocity*)
Plot[u'[y] /. sol, {y, 0, h}, Frame → True,
  PlotStyle → {{Thick, Black}}, LabelStyle → Directive[Black, 12],
  FrameLabel → {"", "", " v ", ""}, FrameStyle → Directive[Thin],
  LabelStyle → Directive[18], Epilog → {Arrow[{{}}, {}], Text[""]}];

```

Out[43]= 0.158941

Out[44]= {0.000010537}



```
In[48]:= u1 = cer2[0, 0, 1];  
0.06 • Spacer2[0];  
0.1
```

In[49]:= a = 0.5;

η = 1;

μ = 1;

k = 2; (\*0,0.2,0.3\*)

b = 0.5;

$$\alpha_1 = \frac{(a^2 - 1) \eta}{(\eta + \mu)}; (*0.1,0.5,1,3*)$$

$$\alpha_2 = (a^2 - 1) \alpha_1;$$

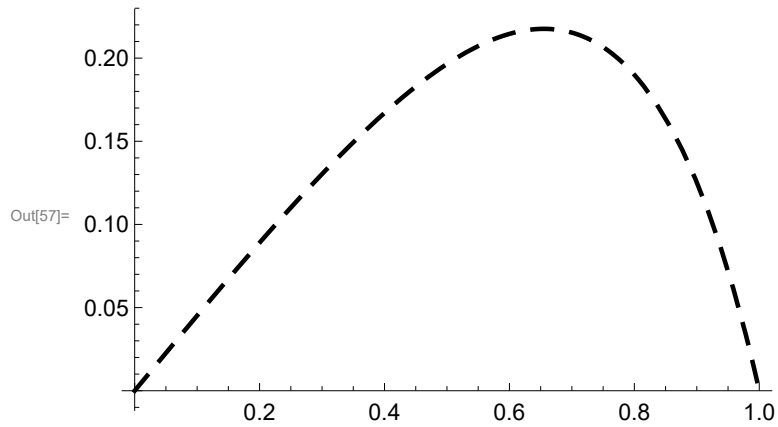
$$pp = -\frac{6(-1+k)(-1+x)x}{(1+k)(k+x-kx)^2} -$$

$$\frac{1}{25k(1+k)^3(k+x-kx)^6} 12b^2(-1+k)(-1+x)x(k^3(79+k(-32+k(77+26k))) - (-1+k)k^2(63+k(55+k(191+91k)))x + 3(-1+k)^2k(29+k(49+k(53+39k))))x^2 - (-1+k)^3(1+5k)(13+k(8+13k))x^3 + (-1+k)^4(13+k(8+13k))x^4) \alpha_1 +$$

$$\frac{1}{30625k^3(1+k)^5(k+x-kx)^{10}} 8b^4(-1+k)(-1+x)x(9(-1+k)^2(26164k^{12}(-2+x)(-1+x)^7 + 26164x^7(1+x) + kx^6(209312 + (26439 - 235201x)x) - k^{11}(-1+x)^6(-550 + x(-443963 + 235201x))) + 2k^{10}(-1+x)^5(-10945 + x(75985 + x(-906523 + 487927x))) + 2k^2x^5(353556 + x(-273280 + x(-557258 + 487927x))) + 4k^6(-1+x)x(-168418 + (-1+x)x(-476296 + (-1+x)x(346861 + 1655413(-1+x)x))) - 5k^3x^4(-282331 + x(438137 + x(341729 + x(-1035337 + 498297x)))) - 5k^9(-1+x)^4(-39505 + x(-8772 + x(225500 + x(-957851 + 498297x)))) + 20k^4x^3(85379 + x(-199689 + x(-23569 + x(560189 + 11x(-58191 + 20203x)))))) + 20k^8(-1+x)^3(-4442 + x(-15499 + x(-38722 + x(222115 + 11x(-42824 + 20203x)))))) + k^5x^2(1427274 + x(-4230511 + 2x(872810 + x(6586595 + x(-13525745 + (10584551 - 3015409x)x)))))) - k^7(-1+x)^2(-202367 + x(234941 + 2x(-92500 + x(-1979055 + x(5834125 + x(-7507903 + 3015409x))))))))) \alpha_1^2 - 250(2k^7(3616 + k(-4429 + k(4302 + k(-3193 + k(2038 + k(1683 + k(-1031 + 689k))))))) - (-1+k)k^6(17267 + k(-21021 + k(15543 + k(-6983 + k(14973 + k(25929 + k(-16843 + 10335k)))))))x + (-1+k)^2k^5(40814 + k(-38829 + k(11524 + k(44317 + k(9938 + k(88291 + k(-59476 + 33761k)))))))x^2 - (-1+k)^3k^4(46410 + k(-31846 + k(-1865 + k(138739 + k(-36884 + k(173044 + 13k(-9125 + 4823k)))))))x^3 + (-1+k)^4k^3(40306 + k(-994 + k(-37264 + k(190331 + k(-92344 + 5k(42550 + k(-29230 + 14469k)))))))x^4 - (-1+k)^5k^2(19292 + k(11438 + k(-58254 + k(155082 + k(-97575 + k(167361 + k(-113837 + 53053k)))))))x^5 + (-1+k)^6k(5512 + k(11044 + k(-38486 + k(78060 + k(-56266 + k(81919 + k(-54688 + 24115k)))))))x^6 - (-1+k)^7(1+9k)(689 + k(-1720 + k(2714 + k(-2228 + k(2714 + k(-1720 + 689k))))))x^7 + (-1+k)^8(689 + k(-1720 + k(2714 + k(-2228 + k(2714 + k(-1720 + 689k))))))x^8) \alpha_2);$$

Plot[pp, {x, 0, 1}, PlotStyle -> {Thickness[0.007], Dashing[.030], Black}, LabelStyle -> Directive[Black, 12]]

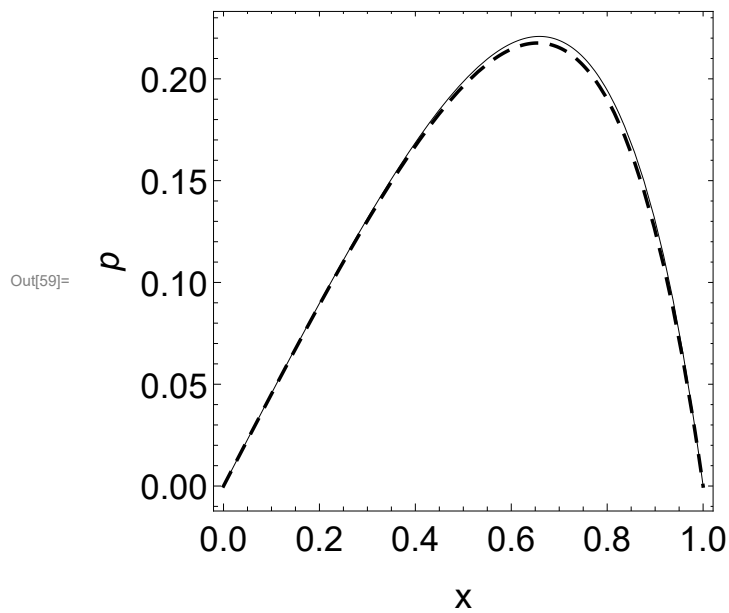


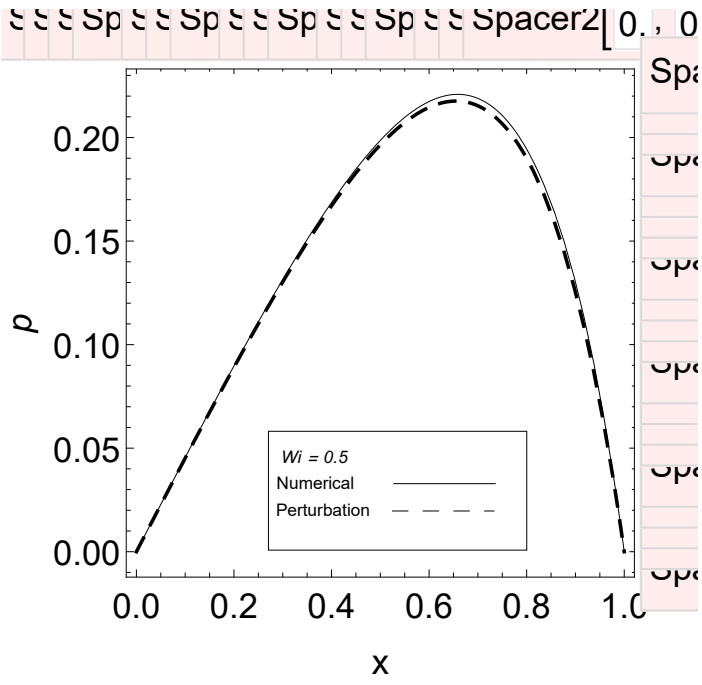


In[58]= `u2 = 0.20` `;`

In[59]= `Show[{u1, u2}, Frame → True, PlotRange → All, LabelStyle → Directive[Black, 18], AspectRatio → 1, FrameLabel → {"x", "p", " a = 0.5, k = 2", ""}, FrameStyle → Directive[Thin], LabelStyle → Directive[Black, 18], Axes → False]`

$a = 0.5, k = 2$



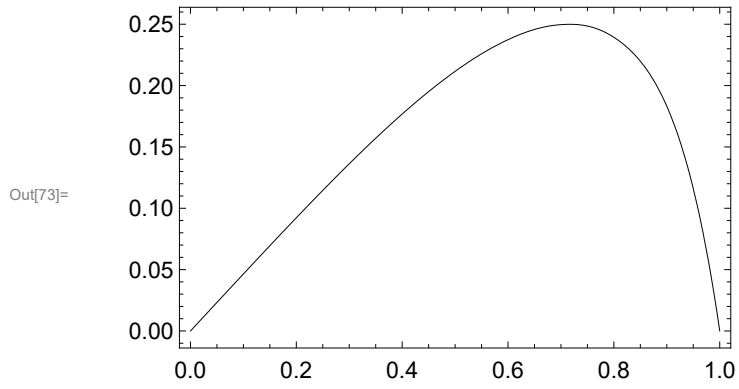


```

In[60]:= k = 2;
a = 0.5;
a1 =  $\frac{(a^2 - 1)}{2}$ ; (*0.1,0.5,1,3*)
a2 = (a^2 - 1) a1;
We = 1;
x[1] = 0;
H = .643699;
For[ii = 1, ii ≤ 11, ii++,
  h = k - (k - 1) * x[ii];
  sol = NDSolve[{D[(u''[y] + We^2 a1 (u''[y])^3 + We^4 a2 (u''[y])^5), y, y] == 0, u[0] == 0,
    u'[0] == 1, u[h] == H, u'[h] == 0}, {u[y], u'[y], u''[y], u'''[y]}, {y, 0, h}];
  ppx = Table[(u(3)[y] + 3 a1 We^2 u''[y]^2 u(3)[y] + 5 a2 We^4 u''[y]^4 u(3)[y]) /. sol,
    {y, 0, h, 0.1}];
  px[ii] = (u(3)[y] + 3 a1 We^2 u''[y]^2 u(3)[y] + 5 a2 We^4 u''[y]^4 u(3)[y]) /. sol /. y → 0;
  x[ii + 1] = x[ii] + 0.1;
];
tt = Table[{x[ii], px[ii][[1]]}, {ii, 1, 11}];
fff = Interpolation[tt];
ggg = Integrate[Interpolation[tt][x], x];
hhh = Integrate[ggg, {x, 0, 1}];
Table[ggg, {x, 1, 1}]
(*pressure*)
Plot[ggg, {x, 0, 1}, Frame → True,
  PlotStyle → {{Thin, Black}}, LabelStyle → Directive[Black, 12],
  FrameLabel → {"", "", " ", ""}, FrameStyle → Directive[Thin],
  LabelStyle → Directive[18], Epilog → {Arrow[{{}}, {}], Text[""]}];
(*pressure gradient*)
Plot[fff[x], {x, 0, 1}, Frame → True, PlotRange → All,
  PlotStyle → {{Thick, Black}}, LabelStyle → Directive[Black, 12],
  FrameLabel → {"", "", " dp/px ", ""}, FrameStyle → Directive[Thin],
  LabelStyle → Directive[18], Epilog → {Arrow[{{}}, {}], Text[""]}];
(*velocity*)
Plot[u'[y] /. sol, {y, 0, h}, Frame → True,
  PlotStyle → {{Thick, Black}}, LabelStyle → Directive[Black, 12],
  FrameLabel → {"", "", " v ", ""}, FrameStyle → Directive[Thin],
  LabelStyle → Directive[18], Epilog → {Arrow[{{}}, {}], Text[""]}];

```

```
Out[72]= {0.0000486587}
```



```
In[76]:= u22 = cer2[0., 0.];  
          0.00 • Spacer2[0  
          0.]
```

In[77]:=  $a = 0.5;$

$\eta = 1;$

$\mu = 1;$

$k = 2; (*0,0.2,0.3*)$

$b = 1;$

$$\alpha_1 = \frac{(a^2 - 1) \eta}{(\eta + \mu)}; (*0.1,0.5,1,3*)$$

$$\alpha_2 = (a^2 - 1) \alpha_1;$$

$$pp = -\frac{6(-1+k)(-1+x)x}{(1+k)(k+x-kx)^2} -$$

$$\frac{1}{25k(1+k)^3(k+x-kx)^6} 12b^2(-1+k)(-1+x)x(k^3(79+k(-32+k(77+26k))) -$$

$$(-1+k)k^2(63+k(55+k(191+91k)))x + 3(-1+k)^2k(29+k(49+k(53+39k)))x^2 -$$

$$(-1+k)^3(1+5k)(13+k(8+13k))x^3 + (-1+k)^4(13+k(8+13k))x^4) \alpha_1 +$$

$$\frac{1}{30625k^3(1+k)^5(k+x-kx)^{10}} 8b^4(-1+k)(-1+x)x$$

$$(9(-1+k)^2(26164k^{12}(-2+x)(-1+x)^7 + 26164x^7(1+x) +$$

$$kx^6(209312 + (26439 - 235201x)x) - k^{11}(-1+x)^6(-550 + x(-443963 + 235201x))) +$$

$$2k^{10}(-1+x)^5(-10945 + x(75985 + x(-906523 + 487927x))) +$$

$$2k^2x^5(353556 + x(-273280 + x(-557258 + 487927x))) + 4k^6(-1+x)x$$

$$(-168418 + (-1+x)x(-476296 + (-1+x)x(346861 + 1655413(-1+x)x))) -$$

$$5k^3x^4(-282331 + x(438137 + x(341729 + x(-1035337 + 498297x)))) -$$

$$5k^9(-1+x)^4(-39505 + x(-8772 + x(225500 + x(-957851 + 498297x)))) +$$

$$20k^4x^3(85379 + x(-199689 + x(-23569 + x(560189 + 11x(-58191 + 20203x)))))) + 20$$

$$k^8(-1+x)^3(-4442 + x(-15499 + x(-38722 + x(222115 + 11x(-42824 + 20203x)))))) +$$

$$k^5x^2(1427274 + x(-4230511 + 2x(872810 + x(6586595 + x(-13525745 +$$

$$(10584551 - 3015409x)x)))) - k^7(-1+x)^2(-202367 + x(234941 +$$

$$2x(-92500 + x(-1979055 + x(5834125 + x(-7507903 + 3015409x)))))) \alpha_1^2 -$$

$$250(2k^7(3616 + k(-4429 + k(4302 + k(-3193 + k(2038 + k(1683 + k(-1031 + 689k))))))) -$$

$$(-1+k)k^6(17267 + k(-21021 + k(15543 + k(-6983 +$$

$$k(14973 + k(25929 + k(-16843 + 10335k))))))x + (-1+k)^2k^5(40814 +$$

$$k(-38829 + k(11524 + k(44317 + k(9938 + k(88291 + k(-59476 + 33761k))))))x^2 -$$

$$(-1+k)^3k^4(46410 + k(-31846 + k(-1865 + k(138739 +$$

$$k(-36884 + k(173044 + 13k(-9125 + 4823k))))))x^3 +$$

$$(-1+k)^4k^3(40306 + k(-994 + k(-37264 + k(190331 + k(-92344 + 5k(42550 +$$

$$k(-29230 + 14469k))))))x^4 - (-1+k)^5k^2(19292 + k(11438 + k$$

$$(-58254 + k(155082 + k(-97575 + k(167361 + k(-113837 + 53053k))))))x^5 +$$

$$(-1+k)^6k(5512 + k(11044 + k(-38486 + k(78060 + k(-56266 +$$

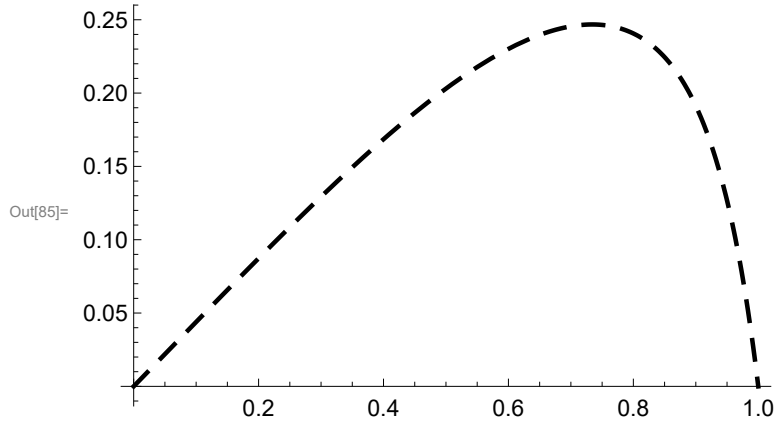
$$k(81919 + k(-54688 + 24115k))))))x^6 - (-1+k)^7(1+9k)$$

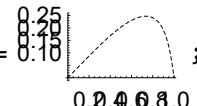
$$(689 + k(-1720 + k(2714 + k(-2228 + k(2714 + k(-1720 + 689k))))))x^7 +$$

$$(-1+k)^8(689 + k(-1720 + k(2714 + k(-2228 + k(2714 + k(-1720 + 689k))))))x^8) \alpha_2);$$

Plot[pp, {x, 0, 1}, PlotStyle -> {Thickness[0.007], Dashing[.030], Black},

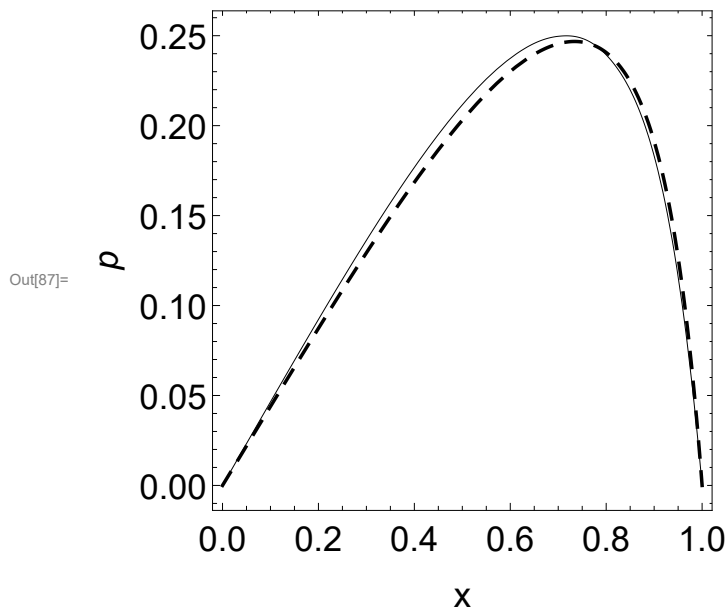
LabelStyle -> Directive[Black, 12]]

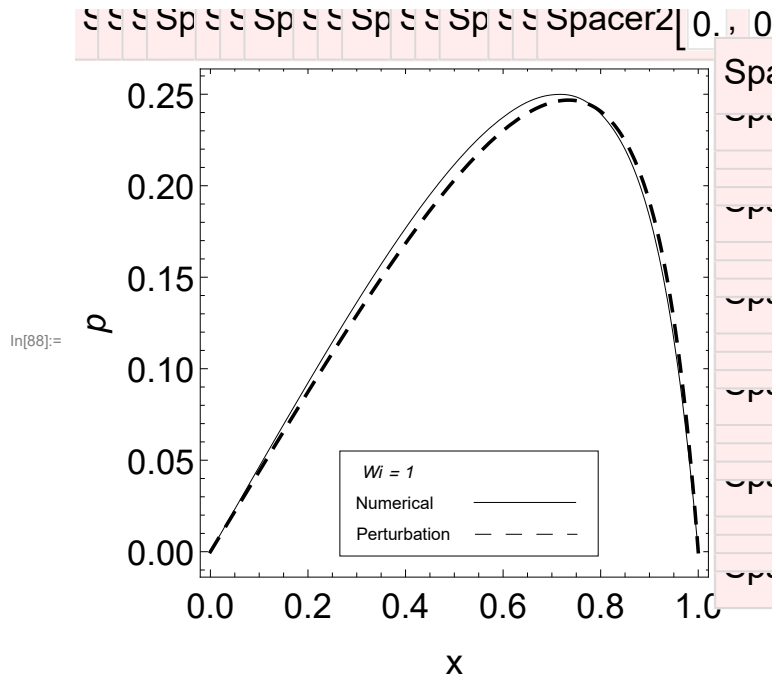


```
In[86]:= u33 =  ;
```

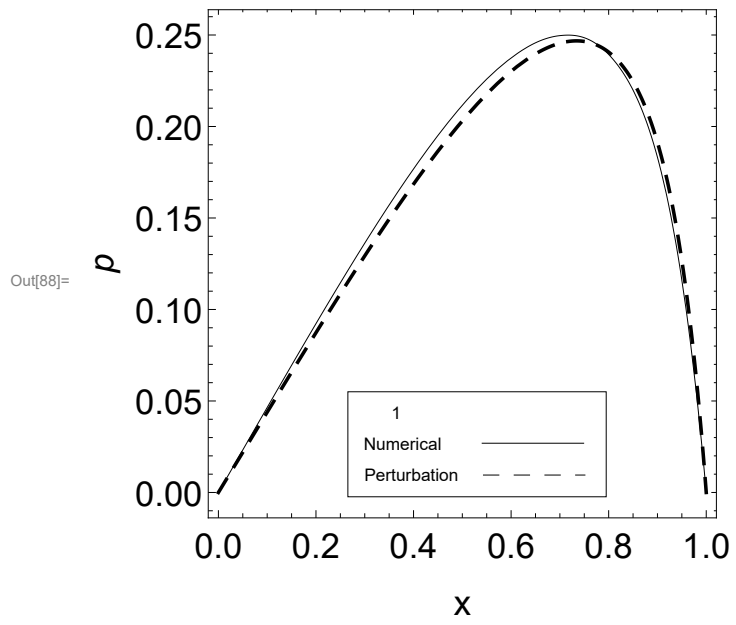
```
In[87]:= Show[{u22, u33}, Frame → True, PlotRange → All, LabelStyle → Directive[Black, 18],
  AspectRatio → 1, FrameLabel → {"x", "p", " a = 0.5, k = 2", ""},
  FrameStyle → Directive[Thin], LabelStyle → Directive[Black, 18], Axes → False]
```

$a = 0.5, k = 2$





$a = 0.5, k = 2$



In[89]= **k = 2;**

**a = 0.5;**

**η = 1;**

**μ = 1;**

$$\alpha_1 = \frac{(a^2 - 1) \eta}{(\eta + \mu)}; (*0.1, 0.5, 1, 3*)$$

$$\alpha_2 = (a^2 - 1) \alpha_1;$$

$$HHH = \frac{k}{1 + k} +$$

$$\left( b^2 \left( \frac{12 \alpha_1}{25 (1+k)^3} + \frac{156 \alpha_1}{25 k^3 (1+k)^3} - \frac{168 \alpha_1}{25 k^2 (1+k)^3} + \frac{12 \alpha_1}{25 k (1+k)^3} - \frac{168 k \alpha_1}{25 (1+k)^3} + \frac{156 k^2 \alpha_1}{25 (1+k)^3} \right) \right) /$$

$$\left( -\frac{36}{(1+k)^3} - \frac{6}{k^2 (1+k)^3} - \frac{24}{k (1+k)^3} - \frac{24 k}{(1+k)^3} - \frac{6 k^2}{(1+k)^3} \right) +$$

$$\left( b^4 \left( -\frac{2640312 \alpha_1^2}{30625 (1+k)^5} - \frac{1883808 \alpha_1^2}{30625 k^5 (1+k)^5} + \frac{3747816 \alpha_1^2}{30625 k^4 (1+k)^5} - \frac{126216 \alpha_1^2}{875 k^3 (1+k)^5} + \frac{5193864 \alpha_1^2}{30625 k^2 (1+k)^5} - \right. \right.$$

$$\frac{2640312 \alpha_1^2}{30625 k (1+k)^5} + \frac{5193864 k \alpha_1^2}{30625 (1+k)^5} - \frac{126216 k^2 \alpha_1^2}{875 (1+k)^5} + \frac{3747816 k^3 \alpha_1^2}{30625 (1+k)^5} - \frac{1883808 k^4 \alpha_1^2}{30625 (1+k)^5} +$$

$$\frac{9344 \alpha_2}{245 (1+k)^5} + \frac{11024 \alpha_2}{245 k^5 (1+k)^5} - \frac{16496 \alpha_2}{245 k^4 (1+k)^5} + \frac{2272 \alpha_2}{35 k^3 (1+k)^5} - \frac{19776 \alpha_2}{245 k^2 (1+k)^5} +$$

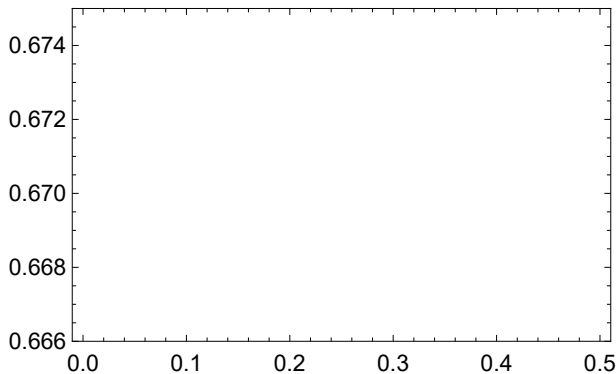
$$\left. \left. \frac{9344 \alpha_2}{245 k (1+k)^5} - \frac{19776 k \alpha_2}{245 (1+k)^5} + \frac{2272 k^2 \alpha_2}{35 (1+k)^5} - \frac{16496 k^3 \alpha_2}{245 (1+k)^5} + \frac{11024 k^4 \alpha_2}{245 (1+k)^5} \right) \right) /$$

$$\left( -\frac{90}{(1+k)^5} - \frac{6}{k^2 (1+k)^5} - \frac{36}{k (1+k)^5} - \frac{120 k}{(1+k)^5} - \frac{90 k^2}{(1+k)^5} - \frac{36 k^3}{(1+k)^5} - \frac{6 k^4}{(1+k)^5} \right)$$

**Plot[HHH, {b, 0, 0.5}, Frame → True, PlotRange → {0.666, .675},  
 PlotStyle → {{Thin, Black}}, LabelStyle → Directive[Black, 12],  
 FrameLabel → {"", ""}, FrameStyle → Directive[Thin],  
 LabelStyle → Directive[18], Epilog → {Arrow[{{}}, {}], Text[""]}]**

Out[95]= 0.662893

Out[96]=

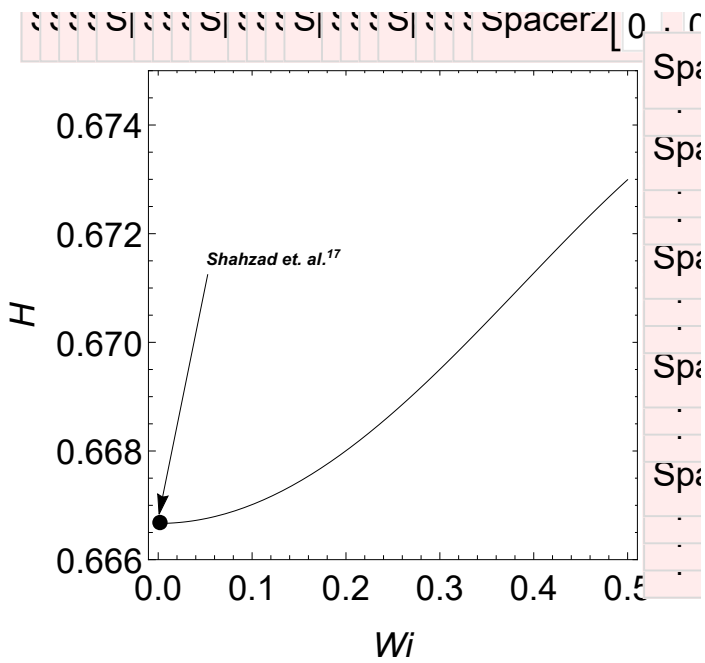
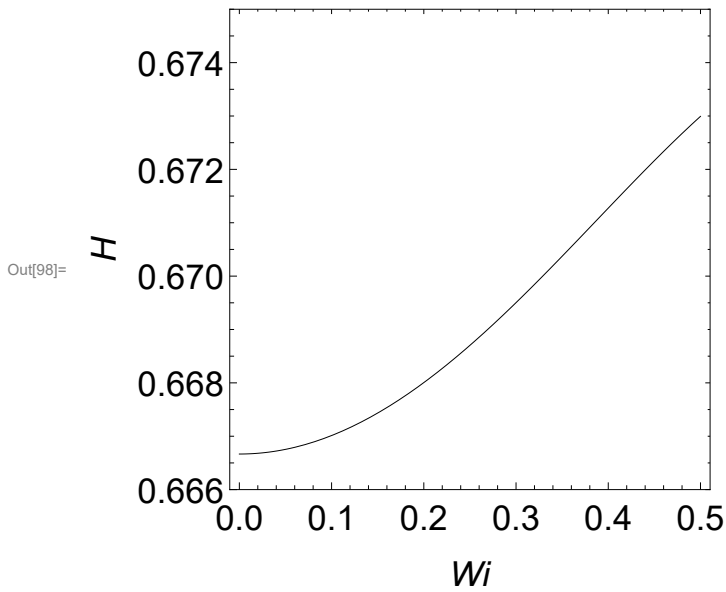


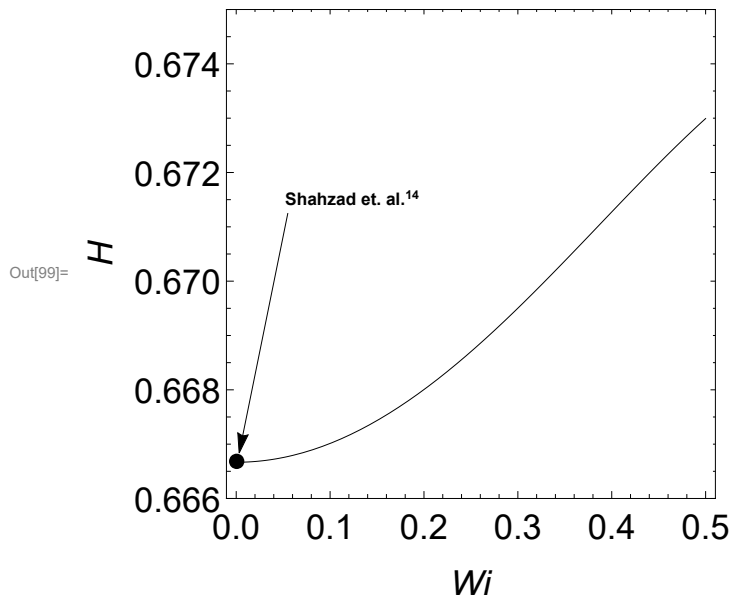
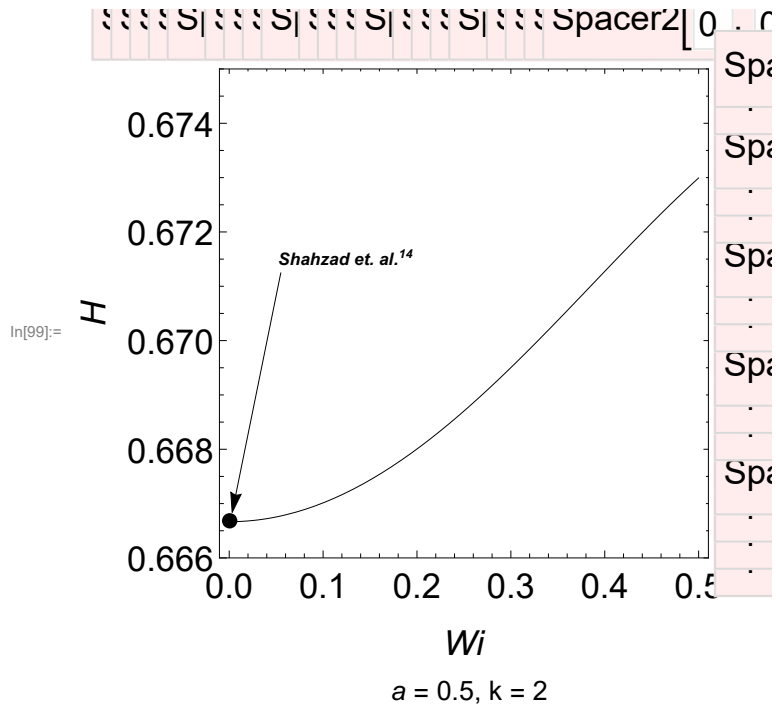


```
In[97]:= n1 =  $\text{Plot}[\text{Function}[Wi, \text{Numerator}[0.666 + \text{Spacer2}[0.01] \cdot Wi^2], \text{Denominator}[0.666 + \text{Spacer2}[0.01] \cdot Wi^2]], \{Wi, 0, 0.5\}];$ 
```

```
In[98]:= Show[{n1}, Frame -> True, PlotRange -> {.666, .675}, LabelStyle -> Directive[Black, 18], AspectRatio -> 1, FrameLabel -> {"Wi", "H", "a = 0.5, k = 2", ""}, FrameStyle -> Directive[Thin], LabelStyle -> Directive[Black, 18], Axes -> False]
```

$a = 0.5, k = 2$





In[100]:=

In[101]:= a = 1;

η = 1;

μ = 1;

k = 6; (\*2,4,6\*)

x = 0.5;

$$\alpha_1 = \frac{(a^2 - 1) \eta}{(\eta + \mu)}; (*0.1, 0.5, 1, 3*)$$

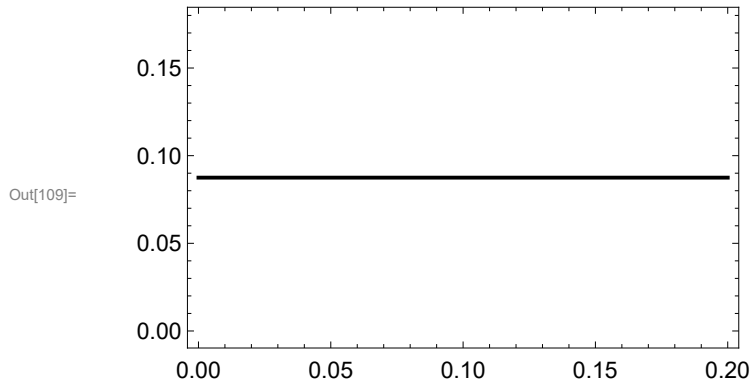
$$\alpha_2 = (a^2 - 1) \alpha_1;$$

$$pp = -\frac{6(-1+k)(-1+x)x}{(1+k)(k+x-kx)^2} -$$

$$\frac{1}{25k(1+k)^3(k+x-kx)^6} 12b^2(-1+k)(-1+x)x(k^3(79+k(-32+k(77+26k))) - (-1+k)k^2(63+k(55+k(191+91k)))x + 3(-1+k)^2k(29+k(49+k(53+39k))))x^2 - (-1+k)^3(1+5k)(13+k(8+13k))x^3 + (-1+k)^4(13+k(8+13k))x^4) \alpha_1 +$$

$$\frac{1}{30625k^3(1+k)^5(k+x-kx)^{10}} 8b^4(-1+k)(-1+x)x(9(-1+k)^2(26164k^{12}(-2+x)(-1+x)^7 + 26164x^7(1+x) + kx^6(209312 + (26439 - 235201x)x) - k^{11}(-1+x)^6(-550 + x(-443963 + 235201x))) + 2k^{10}(-1+x)^5(-10945 + x(75985 + x(-906523 + 487927x))) + 2k^2x^5(353556 + x(-273280 + x(-557258 + 487927x))) + 4k^6(-1+x)x(-168418 + (-1+x)x(-476296 + (-1+x)x(346861 + 1655413(-1+x)x))) - 5k^3x^4(-282331 + x(438137 + x(341729 + x(-1035337 + 498297x)))) - 5k^9(-1+x)^4(-39505 + x(-8772 + x(225500 + x(-957851 + 498297x)))) + 20k^4x^3(85379 + x(-199689 + x(-23569 + x(560189 + 11x(-58191 + 20203x)))))) + 20k^8(-1+x)^3(-4442 + x(-15499 + x(-38722 + x(222115 + 11x(-42824 + 20203x)))))) + k^5x^2(1427274 + x(-4230511 + 2x(872810 + x(6586595 + x(-13525745 + (10584551 - 3015409x)x)))))) - k^7(-1+x)^2(-202367 + x(234941 + 2x(-92500 + x(-1979055 + x(5834125 + x(-7507903 + 3015409x))))))))) \alpha_1^2 - 250(2k^7(3616 + k(-4429 + k(4302 + k(-3193 + k(2038 + k(1683 + k(-1031 + 689k))))))) - (-1+k)k^6(17267 + k(-21021 + k(15543 + k(-6983 + k(14973 + k(25929 + k(-16843 + 10335k)))))))x + (-1+k)^2k^5(40814 + k(-38829 + k(11524 + k(44317 + k(9938 + k(88291 + k(-59476 + 33761k)))))))x^2 - (-1+k)^3k^4(46410 + k(-31846 + k(-1865 + k(138739 + k(-36884 + k(173044 + 13k(-9125 + 4823k)))))))x^3 + (-1+k)^4k^3(40306 + k(-994 + k(-37264 + k(190331 + k(-92344 + 5k(42550 + k(-29230 + 14469k)))))))x^4 - (-1+k)^5k^2(19292 + k(11438 + k(-58254 + k(155082 + k(-97575 + k(167361 + k(-113837 + 53053k)))))))x^5 + (-1+k)^6k(5512 + k(11044 + k(-38486 + k(78060 + k(-56266 + k(81919 + k(-54688 + 24115k)))))))x^6 - (-1+k)^7(1+9k)(689 + k(-1720 + k(2714 + k(-2228 + k(2714 + k(-1720 + 689k))))))x^7 + (-1+k)^8(689 + k(-1720 + k(2714 + k(-2228 + k(2714 + k(-1720 + 689k))))))x^8) \alpha_2);$$

Plot[pp, {b, 0, .2}, Frame → True, PlotStyle → {{Thick, Black}}, LabelStyle → Directive[Black, 12], FrameLabel → {"", "", " ", ""}, FrameStyle → Directive[Thin], LabelStyle → Directive[18], Epilog → {Arrow[{{}}, {}], Text[""]}]



```
In[110]:= o3 = cer2[0, 0.1];  
0.06 • Spacer2[0];  
0.1
```

```
In[111]:= o2 = cer2[0, 0.1];  
0.06 • Spacer2[0];  
0.1
```

```
In[112]:= o1 = cer2[0, 0.1];  
0.8 • Spacer2[0];  
0.1
```

```
In[113]:= Show[{o1, o2, o3}, Frame → True, PlotRange → {0, .3}, LabelStyle → Directive[Black, 18],  
AspectRatio → 1, FrameLabel → {"x", "p", " a = 0.5, k = 2", ""},  
FrameStyle → Directive[Thin], LabelStyle → Directive[Black, 18], Axes → False]
```

$a = 0.5, k = 2$

