

1) A short example:

$$U = \frac{(\lambda + 2\mu)}{2} \left(\sqrt{J_2} \left(\frac{\partial u_\sigma}{\partial \sigma} + \frac{\partial u_\tau}{\partial \tau} + \sqrt{J_3} \frac{\partial u_\phi}{\partial \phi} \right) \right),$$

$$T_{\max} = \frac{1}{2} \rho \omega^2 \iiint_V (u_\sigma^2 + u_\tau^2 + u_\phi^2) d\tau d\sigma d\phi$$

2) what I want to calculate. $L_{\max} = U - T_{\max}$

3) change of variable: $\mathfrak{N} = \frac{\tau}{\tau_R}, \Upsilon = \frac{\sigma}{\sigma_R}, \zeta = \frac{\phi}{\phi_R} \Rightarrow d\tau = \tau_R d\mathfrak{N}, d\sigma = \sigma_R d\Upsilon, d\phi = \phi_R d\zeta$

4) some assumptions:

$$u_\sigma = \sum_{i=0}^I \sum_{j=0}^J \sum_{k=0}^K A_{ijk} \mathfrak{S}_{ijk}(\sigma, \tau, \phi), u_\tau = \sum_{m=0}^M \sum_{n=0}^N \sum_{p=0}^P B_{mnp} \mathfrak{R}_{mnp}(\sigma, \tau, \phi), u_\phi = \sum_{q=0}^Q \sum_{r=0}^R \sum_{s=0}^S C_{qrs} \Gamma_{qrs}(\sigma, \tau, \phi)$$

5) final equation

$$L_{\max} = \frac{(\lambda + 2\mu)}{2} \left(\sqrt{J_2} \left(\frac{\partial u_\sigma}{\partial \sigma} + \frac{\partial u_\tau}{\partial \tau} + \sqrt{J_3} \frac{\partial u_\phi}{\partial \phi} \right) \right) - \frac{1}{2} \rho \omega^2 \iiint_V (u_\sigma^2 + u_\tau^2 + u_\phi^2) d\tau d\sigma d\phi$$

6) so by using these equation:

$$\frac{1}{\sigma_R} \sum_{ijk} A_{ijk} \frac{\partial \mathfrak{S}_{ijk}}{\partial \Upsilon} = \frac{\partial u_\sigma}{\partial \sigma}, u_\sigma = \sum_{ijk} A_{ijk} \mathfrak{S}_{ijk}, \frac{1}{\phi_R} \sum_{ijk} A_{ijk} \frac{\partial \mathfrak{S}_{ijk}}{\partial \zeta} = \frac{\partial u_\sigma}{\partial \phi}$$

$$\frac{1}{\tau_R} \sum_{mnp} B_{mnp} \frac{\partial \mathfrak{R}_{mnp}}{\partial \mathfrak{N}} = \frac{\partial u_\tau}{\partial \tau}, \frac{1}{\phi_R} \sum_{mnp} B_{mnp} \frac{\partial \mathfrak{R}_{mnp}}{\partial \zeta} = \frac{\partial u_\tau}{\partial \phi}, u_\tau = \sum_{mnp} B_{mnp} \mathfrak{R}_{mnp}$$

$$\frac{1}{\phi_R} \sum_{qrs} C_{qrs} \frac{\partial \Gamma_{qrs}}{\partial \zeta} = \frac{\partial u_\phi}{\partial \phi}, u_\phi = \sum_{qrs} C_{qrs} \Gamma_{qrs}, \frac{\partial u_\phi}{\partial \sigma} = \frac{1}{\sigma_R} \sum_{qrs} C_{qrs} \frac{\partial \Gamma_{qrs}}{\partial \Upsilon}, \frac{\partial u_\phi}{\partial \tau} = \frac{1}{\tau_R} \sum_{qrs} C_{qrs} \frac{\partial \Gamma_{qrs}}{\partial \mathfrak{N}}$$

7) so:

$$L_{\max} = \frac{(\lambda + 2\mu)}{2} \left(\sqrt{J_2} \left(\frac{1}{\sigma_R} \sum_{ijk} A_{ijk} \frac{\partial \mathfrak{S}_{ijk}}{\partial \Upsilon} + \frac{1}{\tau_R} \sum_{mnp} B_{mnp} \frac{\partial \mathfrak{R}_{mnp}}{\partial \mathfrak{N}} + \sqrt{J_3} \frac{1}{\phi_R} \sum_{qrs} C_{qrs} \frac{\partial \Gamma_{qrs}}{\partial \zeta} \right) \right) -$$

$$\frac{1}{2} \rho \omega^2 \iiint_V \left(\left(\sum_{ijk} A_{ijk} \mathfrak{S}_{ijk} \right)^2 + \left(\sum_{mnp} B_{mnp} \mathfrak{R}_{mnp} \right)^2 + \left(\sum_{qrs} C_{qrs} \Gamma_{qrs} \right)^2 \right) \tau_R \sigma_R \phi_R d\mathfrak{N} d\Upsilon d\zeta$$

8) now I want to calculate $\frac{\partial L_{\max}}{\partial A_{ijk}}, \frac{\partial L_{\max}}{\partial B_{mnp}}, \frac{\partial L_{\max}}{\partial C_{qrs}}$